

Given the following matrices, simplify the expressions, *no decimals.*

$$A = \begin{bmatrix} 7 & -2 \\ -1 & 0 \end{bmatrix} \quad B = \begin{bmatrix} 3 & 7 \\ -2 & 4 \end{bmatrix} \quad C = \begin{bmatrix} 1 & -5 \\ -3 & 2 \end{bmatrix} \quad D = \begin{bmatrix} 2 & -3 & 1 \\ 4 & 2 & -1 \\ -2 & 3 & -3 \end{bmatrix}$$

$$E = \begin{bmatrix} 4 & 3 & 1 \\ -2 & -1 & -1 \end{bmatrix} \quad F = \begin{bmatrix} 6 & 5 & -2 \\ 2 & 4 & -1 \\ 3 & 1 & 4 \end{bmatrix}$$

1. $A + 2B - 3C$ $\begin{bmatrix} 10 & 27 \\ 4 & 2 \end{bmatrix}$

6. $|C| + |D|$ ~~24~~ -45

2. $-2(FD)$ $\begin{bmatrix} -72 & 28 & -14 \\ -44 & 2 & -2 \\ -4 & -10 & 20 \end{bmatrix}$

7. C^{-1} $\begin{bmatrix} -2/13 & -5/13 \\ -3/13 & -1/13 \end{bmatrix}$

3. A^2 $\begin{bmatrix} 51 & -14 \\ -7 & 2 \end{bmatrix}$

8. D^{-1} $\begin{bmatrix} 3/32 & 3/16 & -1/32 \\ -7/16 & 1/8 & -3/16 \\ -1/2 & 0 & -1/2 \end{bmatrix}$

4. $\frac{1}{2}(AB) - 2(BC)$ $\begin{bmatrix} 9\frac{1}{2} & 4\frac{5}{2} \\ 5\frac{3}{2} & -7\frac{9}{2} \end{bmatrix}$

9. $F \cdot F^{-1}$ $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

5. $(A + B)|C|$ $\begin{bmatrix} -130 & -65 \\ 39 & -52 \end{bmatrix}$

10. $3D - F$ $\begin{bmatrix} 0 & -14 & 5 \\ 10 & 2 & -2 \\ -9 & 8 & -13 \end{bmatrix}$

Write each system as a matrix equation and then solve.

$X = A^{-1} \cdot B$

11. $3x + 2y = -5$
 $4x = 2y + 10$ $(\frac{5}{2}, -\frac{25}{2})$

$$\begin{bmatrix} 3 & 2 \\ 4 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -5 \\ 10 \end{bmatrix}$$

A X = B

13. $-x + y + z = 4$
 $-x + 2y - 3z = -6$ $(1, 2, 3)$
 $2x - 4y + 8z = 18$

$$\begin{bmatrix} -1 & 1 & 1 \\ -1 & 2 & -3 \\ 2 & -4 & 8 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 4 \\ -6 \\ 18 \end{bmatrix} \quad \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

12. $6x + 2 = y$ $6x - y = -2$
 $-18x + 3y = 4$ $-18x + 3y = 4$ \emptyset

$$\begin{bmatrix} 6 & -1 \\ -18 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -2 \\ 4 \end{bmatrix}$$

14. $5x + 3y + 2z = 1$
 $x - 2y - z = -2$ $\Rightarrow x - 2y + z = 2$ $(-1, 0, 3)$
 $-5x - 2y + 2z = 11$

$$\begin{bmatrix} 5 & 3 & 2 \\ 1 & -2 & 1 \\ -5 & -2 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 11 \end{bmatrix}$$