

Solve the following equations for  $0 \leq x < 2\pi$ .

1.  $\cos x - \cos \frac{1}{2}x = 0$

2.  $\sin 2x \cos x = \sin x$

3.  $\cos 3x - \cos^3 x = 3 \sin^2 x \cos x$

4.  $\tan 2x - \tan x = 0$

5.  $\cos 2x - \cos x = 0$

6.  $2 \cos^2 \frac{x}{2} = 1$

7.  $\tan \frac{x}{2} = 4$

8.  $\cos \frac{x}{2} = 1 + \cos x$

9.  $\sin 2x + \sin x = 0$

10.  $\cos^2 x - \cos 2x = 0$

11.  $\frac{\cos 2x}{\cos^2 x} = 1$

12.  $\cos 2x - 1 = \sin^2 x$

13.  $\cos 2x = \cos x$

14.  $\sin 2x - \cos 2x = 1$

15.  $\sin^2 x - 2 = \cos 2x$

16.  $\cot x + \tan x = 2 \csc 2x$

**OMIT # 5 and #7**

(weird decimal answers)

**TRY #11, 15, 16**

**FOR FUN!**

(interesting "answers")

## Answers

1.  $x = 0, \frac{2\pi}{3}, \pi, \frac{4\pi}{3}$

2.  $x = 0, \frac{\pi}{4}, \frac{3\pi}{4}, \pi, \frac{5\pi}{4}, \frac{7\pi}{4}$

3.  $x = 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}$

4.  $x = 0, \pi$

5.  $x = 2.237, 5.379$

6.  $x = \frac{\pi}{2}, \frac{3\pi}{2}$

7.  $x = 2.6516$

8.  $x = \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{3\pi}{2}$

9.  $x = 0, \frac{2\pi}{3}, \pi, \frac{4\pi}{3}$

10.  $x = 0, \pi$

11. no solution

12.  $x = 0, \pi$

13.  $x = 0, \frac{2\pi}{3}, \frac{4\pi}{3}$

14.  $x = \frac{\pi}{4}, \frac{\pi}{2}, \frac{5\pi}{4}, \frac{3\pi}{2}$

15. no solution

16. infinitely many solutions