

Probability Examples

PROBABILITY — example 1

For a “Prix Fixe” meal at a restaurant, patrons are to select an appetizer, a main dish, a side, and a dessert. If the menu offers a choice of 13 appetizers, 10 main dishes, 8 side dishes and 3 desserts, how many meal combinations are possible?

$$\begin{array}{ccccccc} \textcircled{1} & \textcircled{2} & \textcircled{3} & \textcircled{4} & & & \\ 13 & \cdot & 10 & \cdot & 8 & \cdot & 3 & = & \boxed{3,120} \end{array}$$

PROBABILITY — example 2 *(independent events)*

The probability of having identical twins is $1/285$. What is the probability that a couple has three consecutive sets of identical twins?

$$\begin{array}{cccc} \textcircled{1} & \textcircled{2} & \textcircled{3} & \\ \left(\frac{1}{285}\right) & \cdot & \left(\frac{1}{285}\right) & \cdot & \left(\frac{1}{285}\right) \\ = & \left(\frac{1}{285}\right)^3 & = & 0.0000000043 \end{array}$$

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PROBABILITY – example 3

The probability that two people have **different** birthdays is 0.997. What is the probability that two people have the same birthday?

$$1 - 0.997 = \boxed{0.003}$$

$$P(A) + P(\text{not } A) = 1$$

PROBABILITY – example 4

A standard deck of cards has 52 cards (as represented below). If three cards are dealt, what is the probability that all three are Queens?

Sample Space for Choosing a Card from a Deck

Ace	2	3	4	5	6	7	8	9	10	Jack	Queen	King
♥	♥	♥	♥	♥	♥	♥	♥	♥	♥	♥	♥	♥
Ace	2	3	4	5	6	7	8	9	10	Jack	Queen	King
♦	♦	♦	♦	♦	♦	♦	♦	♦	♦	♦	♦	♦
Ace	2	3	4	5	6	7	8	9	10	Jack	Queen	King
♠	♠	♠	♠	♠	♠	♠	♠	♠	♠	♠	♠	♠
Ace	2	3	4	5	6	7	8	9	10	Jack	Queen	King
♣	♣	♣	♣	♣	♣	♣	♣	♣	♣	♣	♣	♣

R R B B
4 suits (♥, ♦, ♠, ♣)
13 cards in each suit
3 face cards (J, Q, K)
in each suit

→ no replacement
(dependent events)

$$\begin{aligned} & \textcircled{1} \quad \textcircled{2} \quad \textcircled{3} \\ & \frac{4}{52} \cdot \frac{3}{51} \cdot \frac{2}{50} \\ & = \frac{24}{132600} \\ & = \boxed{0.00018} \end{aligned}$$

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PROBABILITY – example 5

A pollster must randomly select 3 of 12 available people.
How many different groups of 3 are possible?

Combination

$$\begin{aligned} {}_{12}C_3 &= \frac{12!}{9!3!} = \frac{12 \cdot 11 \cdot 10}{3 \cdot 2 \cdot 1} \\ &= \boxed{220} \end{aligned}$$

PROBABILITY – example 6

The hover-board club must elect 4 officers (president, vice-president, parliamentarian, and secretary) from 16 available candidates. How many different slates are possible if one candidate is elected for each office?

Position matters
permutation

$$\begin{aligned} {}_{16}P_4 &= \frac{16!}{12!} \\ &= 16 \cdot 15 \cdot 14 \cdot 13 \\ &= \boxed{43,680} \end{aligned}$$