

If $A = \{2, 5, 7, 8\}$, $B = \{3, 6, 7, 8\}$, $C = \{1, 4, 5\}$, and $U = \{1, 2, 3, \dots, 8\}$, find each of the following.

$$A' = \{1, 3, 4, 6\}$$

$$C' = \{2, 3, 6, 7, 8\}$$

1. Find C'

$$\{2, 3, 6, 7, 8\}$$

2. Find $A \cup B$

$$\{2, 3, 5, 6, 7, 8\}$$

3. Find $A' \cap C$

$$\{1, 4\}$$

4. Write $|U|$

$$8$$

5. Write $A \oplus C$

$$\{1, 2, 4, 7, 8\}$$

6. Find $A - B$

$$\{2, 5\}$$

7. Find $B - C$

$$\{3, 6, 7, 8\}$$

8. Find $|C'|$

$$5$$

What can be said about sets A and B if each of the following is true? Think about all possibilities!

9. $A \cup B = A$

$$B \subseteq A \text{ OR } B = \emptyset$$

10. $A \cap B = A$

$$A \subseteq B \text{ OR } A = \emptyset$$

11. $A - B = A$

$$A \text{ and } B \text{ are disjoint.}$$

$$\text{OR } B = \emptyset$$

12. $A - B = B - A$

$$A = B$$

13. $A \cup \emptyset = B$

$$A = B$$

14. $A \cap \emptyset = B$

$$B = \emptyset$$

Multisets

Let $A = \{3 \cdot a, 4 \cdot b, 1 \cdot c\}$ and $B = \{2 \cdot a, 2 \cdot b, 4 \cdot c\}$. Find each of the following:

15. $A \cup B$

$$\{3 \cdot a, 4 \cdot b, 4 \cdot c\}$$

16. $A \cap B$

$$\{2 \cdot a, 2 \cdot b, 1 \cdot c\}$$

17. $A - B$

$$\{1 \cdot a, 2 \cdot b\}$$

18. $B - A$

$$\{3 \cdot c\}$$

19. $A + B$

$$\{5 \cdot a, 6 \cdot b, 5 \cdot c\}$$

20. $|A|$

$$8$$

Suppose that the math department and the science department are ordering technology. Let M be the multiset that the math department needs, $M = \{8 \cdot \text{computers}, 6 \cdot \text{monitors}, 5 \cdot \text{printers}, 105 \cdot \text{calculators}\}$. Let S be the multiset that the science department needs, $S = \{5 \cdot \text{computers}, 5 \cdot \text{monitors}, 7 \cdot \text{printers}, 4 \cdot \text{scanners}\}$.

21. What combination of M and S represents the equipment that should be purchased assuming both departments share equipment?

$$M \cup S = \{8 \cdot c, 6 \cdot m, 7 \cdot p, 4 \cdot s, 105 \cdot \text{calc}\}$$

22. What combination of M and S represents the equipment that the department will share?

$$M \cap S = \{5 \cdot c, 5 \cdot m, 5 \cdot p\}$$

23. What combination of M and S represents the equipment that, if they share, can still be housed in the math department, because the science department won't need it?

$$M - S = \{3 \cdot c, 1 \cdot m, 105 \cdot \text{calc}\}$$

24. What combination of M and S represents the equipment that should be purchased if the departments don't share equipment?

$$M + S = \{13 \cdot c, 11 \cdot m, 12 \cdot p, 4 \cdot s, 105 \cdot \text{calc}\}$$