

Solving Trig Equations using Sum & Difference Identities Notes

Ex.1 - Solve:

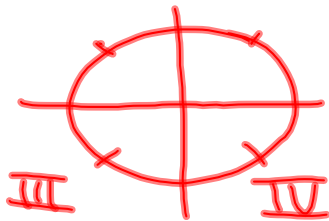
$$\cos\left(\frac{\pi}{2} + x\right) = \frac{\sqrt{2}}{2}$$



$$\cancel{\left(\cos\frac{\pi}{2}\right)\cos x} - \left(\sin\frac{\pi}{2}\right)\sin x = \frac{\sqrt{2}}{2}$$

$$-\sin x = \frac{\sqrt{2}}{2}$$

$$\sin x = -\frac{\sqrt{2}}{2}$$

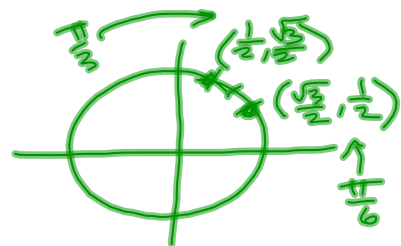


$$x = \frac{5\pi}{4}, \frac{7\pi}{4}$$

- ① expand
- ② substitute & simplify
- ③ solve

Ex.2 - Solve:

$$\cos\left(\frac{\pi}{6} + x\right) + \sin\left(\frac{\pi}{3} + x\right) = 0$$



$$\left(\cos\frac{\pi}{6}\right)\cos x - \left(\sin\frac{\pi}{6}\right)\sin x + \left(\sin\frac{\pi}{3}\right)\cos x + \left(\cos\frac{\pi}{3}\right)\sin x = 0$$

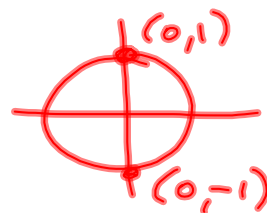
$$\frac{\sqrt{3}}{2}\cos x - \frac{1}{2}\sin x + \frac{\sqrt{3}}{2}\cos x + \frac{1}{2}\sin x = 0$$

$$2\left(\frac{\sqrt{3}}{2}\cos x\right) = 0$$

$$\sqrt{3}\cos x = 0$$

$$\cos x = 0$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}$$



Ex.3 - Solve:

$$\sin(\pi - x) = \sqrt{2} - \sin x$$



$$\cancel{(\sin \pi) \cos x} - (\cos \pi) \sin x = \sqrt{2} - \sin x$$

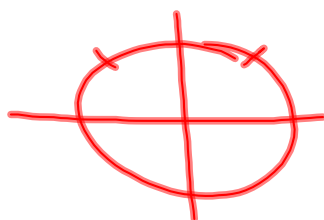
$$- (-1) \cdot \sin x$$

$$\sin x = \sqrt{2} - \cancel{\sin x}$$

$$+ \sin x \quad + \sin x$$

$$2 \sin x = \sqrt{2}$$

$$\sin x = \frac{\sqrt{2}}{2}$$



$$x = \frac{\pi}{4}, \frac{3\pi}{4}$$

Ex.4 - Solve:

$$\cos\left(x + \frac{3\pi}{2}\right) = 2 \sin^2 x - 3$$



$$\cancel{\cos x} \cdot \left(\cos \frac{3\pi}{2}\right) - \sin x \left(\sin \frac{3\pi}{2}\right) = 2 \sin^2 x - 3$$

$$-1$$

$$\sin x = 2 \sin^2 x - 3$$

$$0 = 2 \sin^2 x - \sin x - 3$$

$$0 = (2 \sin x - 3)(\sin x + 1)$$

$$\cancel{\sin x = \frac{3}{2}}$$

N/A

$$\sin x = -1$$

$$x = \frac{3\pi}{2}$$